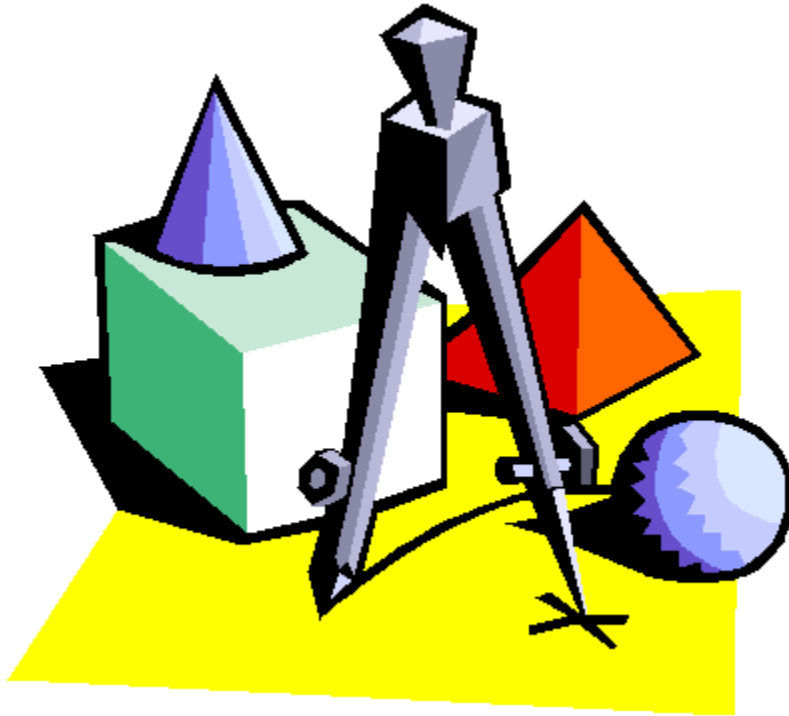


Summer Math Packet



For Students Entering Honors Geometry

Honors Geometry Summer Packet

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Summer Mathematics Packet

Fraction Operations

Exercises: Perform the indicated operation

1. $\frac{6}{7} + \frac{2}{3} =$

2. $\frac{8}{9} + \frac{3}{4} =$

3. $\frac{9}{11} - \frac{2}{5} =$

4. $\frac{5}{7} - \frac{5}{9} =$

5. $\frac{6}{11} \cdot \frac{2}{3} =$

6. $\frac{7}{9} \cdot \frac{3}{5} =$

7. $\frac{6}{7} \div \frac{1}{5} =$

8. $\frac{7}{11} \div \frac{3}{5} =$

9. $3\frac{1}{2} + 5\frac{3}{5} =$

10. $6\frac{17}{25} + 8\frac{4}{7} =$

11. $6\frac{2}{3} + 9\frac{7}{9} =$

12. $8\frac{3}{10} - 6\frac{7}{9} =$

13. $9\frac{7}{15} - 2\frac{7}{12} =$

14. $12\frac{8}{9} - 7\frac{3}{4} =$

15. $6\frac{2}{3} \cdot 7\frac{3}{7} =$

16. $3\frac{1}{3} \cdot 6\frac{4}{5} =$

17. $7\frac{1}{8} \cdot 6 =$

18. $4\frac{1}{4} \div \frac{5}{7} =$

19. $3\frac{2}{3} \div 4\frac{3}{7} =$

20. $\frac{3}{4} \div 2\frac{3}{11} =$

21. $6\frac{1}{5} \div 8\frac{2}{5} =$

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Order of Operations

Evaluate each expression.

1. $8 + 14 - 2 + 4 \times 2^3$

2. $30 - 3^3 + 8 \times 3 \div 12$

3. $3[16 - (3 + 7) \div 5]$

4. $16 \div 4(2) \times 9$

5. $[1 + 3(9 + 12)] - 4^3$

6. $18 \times 3 \div 3^3$

7. $8^2 - 1 \times 3 - 5$

8. $85 - (4 \times 2)^2 - 3 \times 7$

9. $20 - (3^5 \div 27) \times 2$

10. $10 + 5^3 - 25$

11. $6 \div (17 - 11) \times 14$

12. $(9 + 7)^2 \div 4 \times (2 \times 3)$

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Proportions

Solve each proportion for the missing term.

$$1. \frac{4}{x} = \frac{2}{10}$$

$$2. \frac{1}{y} = \frac{3}{15}$$

$$3. \frac{6}{5} = \frac{x}{15}$$

$$4. \frac{20}{28} = \frac{n}{21}$$

$$5. \frac{6}{8} = \frac{7}{a}$$

$$6. \frac{16}{7} = \frac{9}{n}$$

$$7. \frac{1}{0.19} = \frac{12}{n}$$

$$8. \frac{2}{0.21} = \frac{8}{n}$$

9. Seth earns \$152 in 4 days. At that rate, how many days will it take to earn \$532?
10. Lanette drove 248 miles in 4 hours. At that rate, how long will it take her to drive an additional 93 miles?
11. A blueprint for a house states 2.5 inches equals 10 feet. If the length of the wall is 12 feet, how long is the wall in the blueprint?

Squares, Square Roots, and the Laws of Exponents

Hints/Guide:

Exponents are a way to represent repeated multiplication, so that 3^4 means 3 multiplied four times, or $3 \cdot 3 \cdot 3 \cdot 3$, which equals 81. In this example, 3 is the base and 4 is the power.

Roots are the base numbers that correspond to a given power, so the square (referring to the power of 2) root of 81 is 9 because $9 \cdot 9 = 81$ and the fourth root of 81 is 3 because $3 \cdot 3 \cdot 3 \cdot 3$ is 81.

$\sqrt[n]{x}$, where n is the root index and x is the radicand

There are certain rules when dealing with exponents that we can use to simplify problems. They are:

Adding powers	$a^m a^n = a^{m+n}$
Multiplying powers	$(a^m)^n = a^{mn}$
Subtracting powers	$\frac{a^m}{a^n} = a^{m-n}$
Negative powers	$a^{-n} = \frac{1}{a^n}$
To the zero power	$a^0 = 1$

Exercises: Evaluate:

- | | | |
|-----------------------|------------------------------|------------------------------|
| 1. $(8 - 4)^2 =$ | 2. $(4 - 2)^2 (5 - 8)^3 =$ | 3. $5 (8 - 3)^2 =$ |
| 4. $\sqrt{25 - 16} =$ | 5. $\sqrt{5(9 \cdot 125)} =$ | 6. $\sqrt{(8 - 4)(1 + 3)} =$ |

Simplify the following problems using exponents (Do not multiply out):

- | | |
|---------------------------|--------------------------------|
| 7. $5^2 5^4 =$ | 8. $(12^4)^3 =$ |
| 9. $5^9 \div 5^4 =$ | 10. $10^3 \div 10^{-5} =$ |
| 11. $7^{-3} =$ | 12. $3^{-4} =$ |
| 13. $(3^3 \cdot 3^2)^3 =$ | 14. $5^3 \cdot 5^4 \div 5^7 =$ |

Simplifying Radicals

Hints/Guide:

To simplify radicals, first factor the radicand as much as possible, then "pull out" square terms using the following rules:

$$\sqrt{a^2} = a$$

$$\sqrt{ab} = \sqrt{a}\sqrt{b}$$

$$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}} \text{ as long as } b \neq 0$$

A radical is in simplest form when:

- there is no integer under the radical sign with a perfect square factor,
- there are no fractions under the radical sign, and
- there are no radicals in the denominator.

Exercises: Simplify each expression.

1. $\sqrt{\frac{15}{81}} =$

2. $\sqrt{24} + 5\sqrt{6} =$

3. $\sqrt{75} + \sqrt{243} =$

4. $4 + 2\sqrt{10} =$

5. $\sqrt{28} + \sqrt{7} =$

6. $\sqrt{\frac{27}{49}} =$

7. $5\sqrt{3} - \sqrt{75} =$

8. $4\sqrt{3} \cdot \sqrt{18} =$

9. $\sqrt{128} - \sqrt{8} =$

10. $(5\sqrt{3})^2 =$

11. $\sqrt{128} + \sqrt{50} =$

12. $\sqrt{75} \cdot \sqrt{27} =$

13. Nina says that $16 + 4\sqrt{2}$ cannot be simplified. George says that it can be simplified to $20\sqrt{2}$. Who is correct? Explain how you know.

Solving Equations I

Hints/Guide:

The key in equation solving is to isolate the variable, to get the letter by itself. In two-step equations, we must undo addition and subtraction first, then multiplication and division. Remember the golden rule of equation solving: If we do something to one side of the equation, we must do the exact same thing to the other side. Examples:

1. $4x - 6 = -14$

$$+ 6 \quad + 6$$

$$\underline{4x} = \underline{-8}$$

$$4 \quad 4$$

$$x = -2$$

$$\text{Solve: } 4(-2) - 6 = -14$$

$$-8 - 6 = -14$$

$$-14 = -14$$

2. $\frac{x}{-6} - 4 = -8$

$$+ 4 \quad + 4$$

$$-6 \cdot \frac{x}{-6} = -4 \cdot -6$$

$$x = 24$$

$$\text{Solve: } (24/-6) - 4 = -8$$

$$-4 - 4 = -8$$

$$-8 = -8$$

When solving equations that include basic mathematical operations, we must simplify the mathematics first, then solve the equations. For example:

$$5(4 - 3) + 7x = 4(9 - 6)$$

$$5(1) + 7x = 4(3)$$

$$5 + 7x = 12$$

$$-5 \quad -5$$

$$\underline{7x} = \underline{7}$$

$$x = 1$$

$$\text{Check: } 5(4 - 3) + 7(1) = 4(9 - 6)$$

$$5 + 7 = 4(3)$$

$$12 = 12$$

Exercises: Solve the following equations using the rules listed on the previous pages:

1. $-4t + 3t - 8 = 24$

2. $\frac{m}{-5} + 6 = 4$

3. $-4r + 5 - 6r = -32$

4. $\frac{x}{-3} + (-7) = 6$

5. $6g + (-3) = -12$

6. $\frac{y}{-2} + (-4) = 8$

7. $9 - 5(4 - 3) = -16 + \frac{x}{3}$

8. $6t - 14 - 3t = 8(7 - (-2))$

9. $7(6 - (-8)) = \frac{t}{-4} + 2$

10. $7(3 - 6) = 6(4 + t)$

11. $4r + 5r - 8r = 13 + 6$

12. $3(7 + x) = 5(7 - (-4))$

13. Explain in words how to solve a two step equation, similar to any of the equations in problems 2 through 6 above.

Solving Equations II

Hints/Guide:

As we know, the key in equation solving is to isolate the variable. In equations with variables on each side of the equation, we must combine the variables first by adding or subtracting the amount of one variable on each side of the equation to have a variable term on one side of the equation. Then, we must undo the addition and subtraction, then multiplication and division. Remember the golden rule of equation solving. Examples:

$$\begin{array}{r} 8x - 6 = 4x + 5 \\ - 4x \quad - 4x \\ \hline 4x - 6 = 5 \\ + 6 \quad + 6 \\ \hline 4x = 11 \\ 4 \quad 4 \\ \hline x = 2\frac{3}{4} \end{array}$$

$$\begin{array}{r} 5 - 6t = 24 + 4t \\ + 6t \quad + 6t \\ \hline 5 = 24 + 10t \\ - 24 \quad - 24 \\ \hline -19 = 10t \\ 10 \quad 10 \\ \hline -1\frac{9}{10} = t \end{array}$$

Exercises: Solve the following problems:

1. $4r - 7 = 6r + 16 - 3r$ 2. $13 + 3t = 5t - 9$ 3. $-3x + 5 = 3x - 3$

4. $6y + 5 = 6y - 15$ 5. $5x - 8 = 6 - 7x + 2x$ 6. $7p - 8 = -6p + 8$

7. **Rowboat Rentals:** \$5.00 per hour plus a \$100.00 deposit. *Deposit will be refunded if the boat is returned undamaged.*

Which equation represents the total cost for renting and returning a row-boat undamaged? Let c be the total cost in dollars and t be the time in hours.

- a. $c = 5t + 100$ b. $c = 500t$
- c. $c = 100t + 5$ d. $c = 5t$

8. Ted wants to buy a \$400.00 bike. He has two options for payment.

Option One: Ted can borrow the \$400.00 from his father and repay him \$40.00 a month for a year.

Option Two: The bike shop will finance the bike for one year at a 15% annual interest rate. The formula for the total amount paid (a) is:

$$a = p + prt, \text{ where } p \text{ is the amount borrowed, } r \text{ is the rate of interest, and } t \text{ is the time in years.}$$

Which option would cost Ted the least amount of money?

Explain how you determined your answer. Use words, symbols, or both in your explanation.

Factoring Quadratic Equations

Hints/Guide:

Factoring a polynomial can make a problem easier to solve or allow one to easily find the roots of an equation. Factoring can be thought of as the opposite of distribution because terms are expanded, usually from a trinomial (three term) equation to an equation which is the product of two binomial (two) terms.

Examples: $x^2 + 5x + 6 = (x + 2)(x + 3)$
 $2x^2 - 3x - 2 = (2x + 1)(x - 2)$

If these equations are set to zero, then we can solve for the roots of the equation by setting each binomial term to zero.

Example: $2x^2 - 3x - 2 = 0$ $(2x + 1)(x - 2) = 0$
 which means that $2x + 1 = 0$ or $x - 2 = 0$ because if the product is zero,
 then one of the factors must be zero.
 therefore, $x = -0.5$ or $x = 2$.

Exercises: Find the roots of each equation.

1. $a^2 + a - 30 = 0$

2. $b^2 + 7b + 12 = 0$

3. $m^2 - 14m + 40 = 0$

4. $s^2 + 3s - 180 = 0$

5. $7a^2 + 22a + 3 = 0$

6. $2x^2 - 5x - 12 = 0$

7. $4n^2 - 4n - 35 = 0$

8. $72 - 26y + 2y^2 = 0$

9. $10 + 19m + 6m^2 = 0$

10. $x^2 - 2x = 15$

11. $2x^2 + x = 3$

12. $3x^2 - 4x = 4$

Solving Systems of Equations

Hints/Guide:

A system of equations occurs when a situation involves multiple components that can individually be described using equations. Where these equations intersect, their x and y values are the same. Graphically, this appears as an intersection of lines. Algebraically, the x and y values that solve simultaneous equations are the same. The three primary methods of solving systems of equations are graphically, by substitution, and by linear combination.

Exercises: Solve each system of equations using any method.

1. $3x - 4y = 3$
 $6x + 8y = 54$

2. $9 = 5x + 2y$
 $-31 = 3x - 4y$

3. $2x - 7y = 19$
 $-6x - 21y = -15$

4. $4x - 11y = -9$
 $-6x + 22y = 8$

5. Hanz and Mario went to a sale at a music store where all CDs were one price and all cassettes were another price. Hanz bought 2 CDs and 2 cassettes for \$40.00, while Mario bought 1 CD and 4 cassettes for \$44.00.

The equations below represent these purchases, where x is the cost of a CD and y is the cost of a cassette.

Hanz $2x + 2y = 40$

Mario $x + 4y = 44$

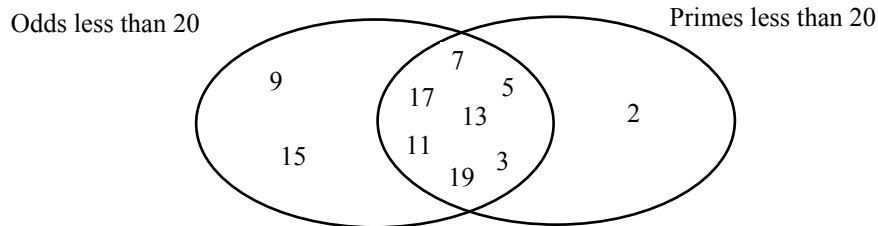
What are the costs of a single CD and a single cassette? Solve the system of equations by either constructing a graph on a sheet of graph paper or by using an algebraic process. Explain how you determined the costs. Use words, symbols, or both in your explanation.

6. An exam will have 20 questions and be worth a total of 100 points. There will be a true/false section where the questions are worth 3 points each and a short essay section where the questions will be worth 11 points each. How many essay questions will there be on the test?

Venn Diagrams

Hints/Guide:

Venn Diagrams can be used to aid on solving problems involving sets. Venn Diagrams can be used to show the relationships between sets, such as between odd numbers less than 20 and prime numbers less than 20:



Notice how, in the example, numbers that are in both sets are listed in the intersection of the two circles. By using this in solving problems, we can eliminate the problem of counting an item or person twice that may appear in more than one set.

Exercises:

1. On one particular day, 49 people purchased drinks from a vending machine. If 27 people purchased Mighty Grape Soda and 30 purchased Tree Root Beer, how many people purchased both?

2. While watching the Staff-Student Basketball Game, 30 fans cheered for the Staff, 50 cheered for the Students, and 17 cheered for both. If there were 65 fans watching the game, how many people cheered for neither?

3. In a recent sixth grade survey, out of 324 students, the following information was collected regarding condiments for hot dogs. The results were: 144 liked mustard, 241 liked ketchup, 97 liked pickle relish, 49 liked ketchup and pickle relish but not mustard, 14 liked mustard and pickle relish but not ketchup, 81 like mustard and ketchup but not pickle relish, and 32 like only mustard.
 - a. How many do not like any of these three condiments on their hot dog?

 - b. How many like exactly one of these three on their hot dog?

 - c. How many like exactly two of these three on their hot dog?

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Probability

Hints/Guide:

Probability is the number of times something will happen compared to the total number of possibilities. Probability can be expressed as a fraction, a ratio, or a percent, and always is between 0 and 1.

Exercises:

1. All 15 students in Joe's English class must give an oral report. The teacher randomly selects 1 student each day to present his or her report. If by the end of the third day Joe has not been selected, what is the probability that the teacher will select Joe on the fourth day?

2. The table below shows the results of a survey given to 100 randomly selected seniors at Willis High School concerning their plans after graduation.

Activity	Number of Students
Attend 2-year college	36
Attend 4-year college	21
Attend technical school	17
Join the military	5
Work full time	14
Other	7

Use this data to predict the probability that a senior at Willis High School plans to join the military after graduation.

3. If a computer randomly chooses a letter in the word "probability," what is the probability it will select a

- | | | | |
|--------|--------|--------|--------|
| a. p ? | b. r ? | c. b ? | d. a ? |
| e. i ? | f. y ? | | |

4. If a card is selected at randomly from a deck of 52 standard playing cards, what is the probability of selecting

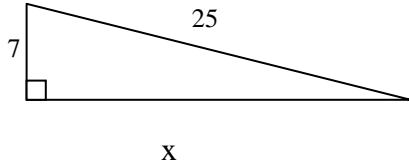
- | | |
|------------------------|--------------------|
| a. a red queen? | b. a black card? |
| c. the jack of hearts? | d. a prime number? |

Pythagorean Theorem

Hints/Guide:

The Pythagorean Theorem states that in a right triangle, and only in a right triangle, the length of the longest side (the side opposite the right angle and called the hypotenuse, or c in the formula) squared is equal to the sum of the squares of the other two sides (the sides that meet to form the right angle called legs, or a and b in the formula). The formula is $a^2 + b^2 = c^2$.

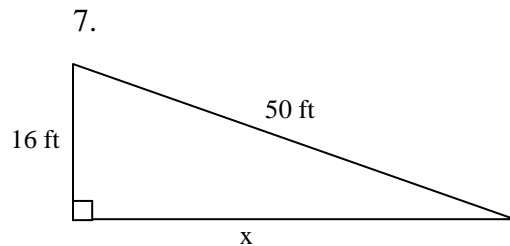
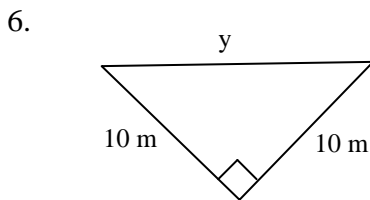
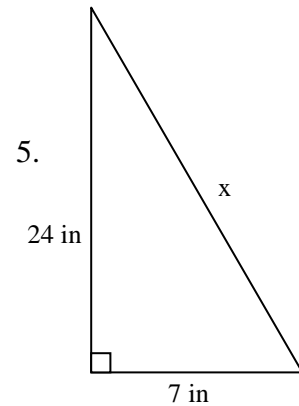
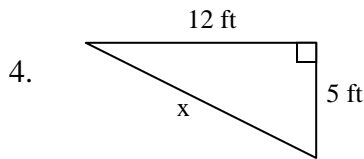
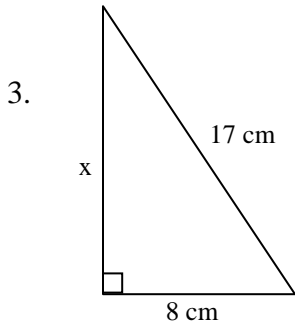
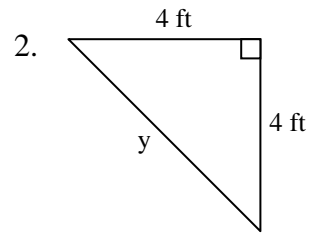
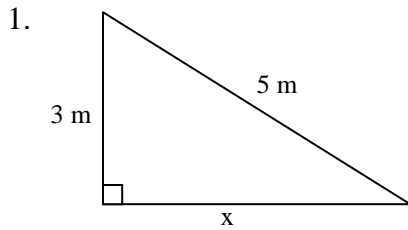
Find the missing side.



$$\begin{aligned}
 a^2 + b^2 &= c^2 \\
 7^2 + x^2 &= 25^2 \\
 49 + x^2 &= 625 \\
 -49 &\quad -49 \\
 x^2 &= 576 \\
 \sqrt{x^2} &= \sqrt{576} \\
 x &= 24
 \end{aligned}$$

Exercises: Solve for the variable:

SHOW ALL WORK. Use a separate sheet of paper (if necessary) and staple to this page.



Distance and Midpoint Formulas

Hints/Guide:

To find the distance between two points, we use the distance formula, which is:

$$Distance = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

To find the midpoint of two points, we use the midpoint formula, which is:

$$Midpoint = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

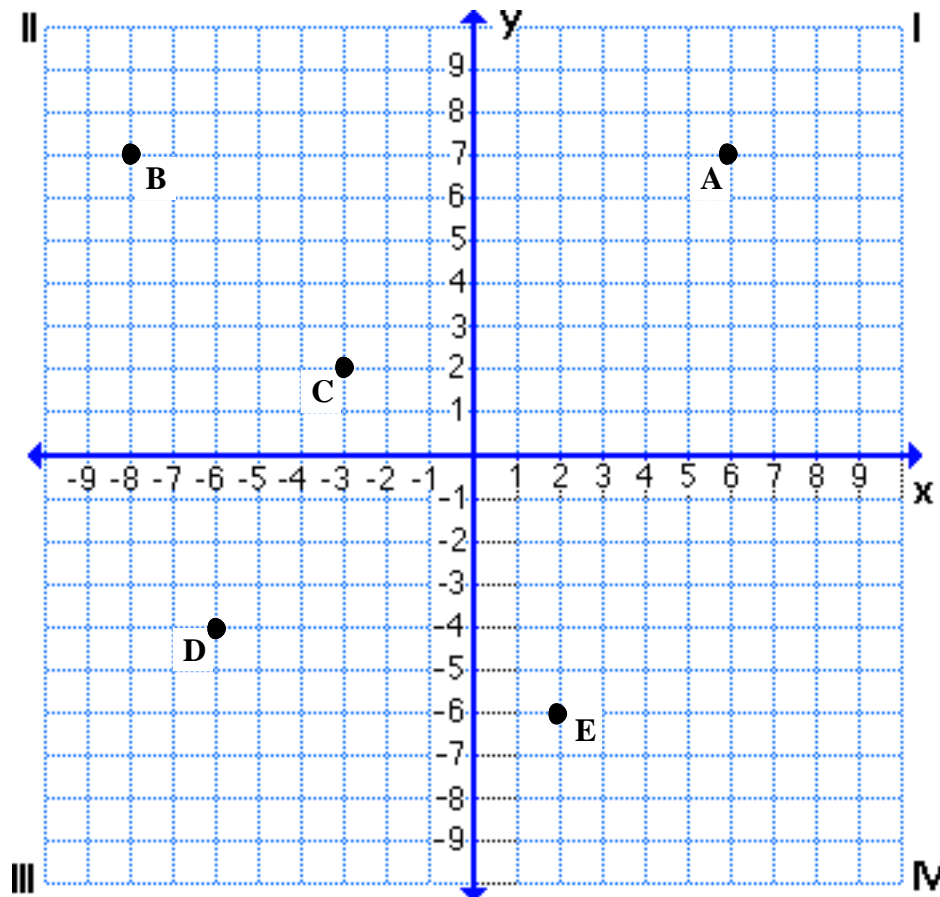
Exercises:

1. Find the distance between points

- a. A and B b. C and E c. D and E d. A and E

2. Find the midpoint of segment

- a. AB b. CE c. DE d. AE



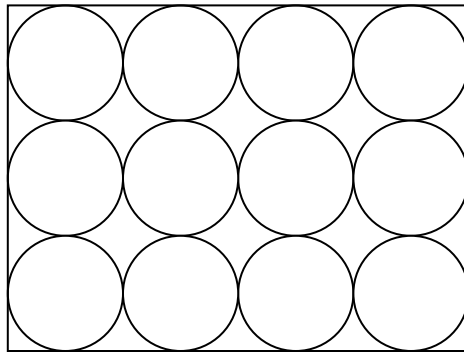
Irregular Area

Hints/Guide:

To solve problems involving irregular area, use either an additive or a subtractive method. In an additive area problem, break the object down into know shapes and then add the areas together. In a subtractive area problem, subtract the area of known shapes from a larger whole.

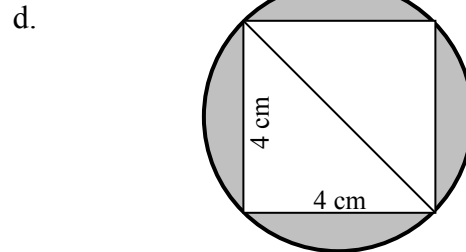
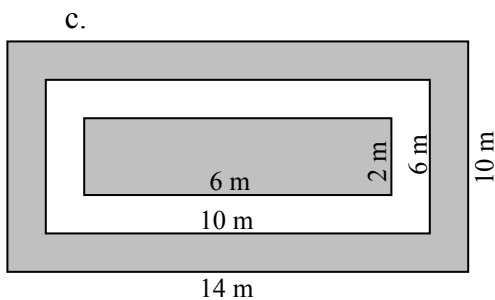
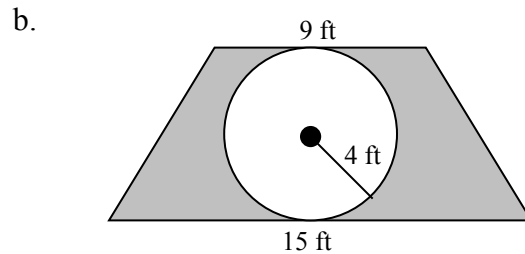
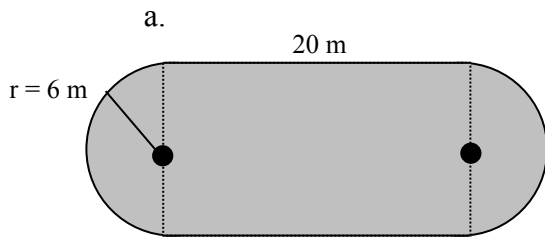
Exercises:

1. The baking sheet shown holds 12 cookies. Each cookie has a diameter of 3 inches.



What is the area of the unused part of the baking sheet? Round your answer to the nearest square inch.

2. Find the area of the shaded regions.



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Problem Solving

1. Brandon's back yard is in the shape of a rectangle. The length is 50 feet and the width is 30 feet. What is the perimeter? What is the area? If you put up a fence and each section is 8 feet long, how many sections would you need and how many posts?
2. Tim is putting in a circular garden in front of his house. He needs to put a low fence around it. He also needs to get mulch. If the circle has a diameter of 12 feet, how much fencing would he need? It comes in rolls of 10 feet. How many rolls will he need? Each bag of mulch covers 3 square feet. How many bags of mulch does he need?
3. Syreeta is having a party. She needs to buy ice cream. She knows that each person needs 2 scoops. The ice cream package is in the shape of a rectangular prism. The length is 12 inches, the height is 5 inches, and the width is 8 inches. What is the volume? If each scoop is around 12 cubic inches, how many scoops can I get out of a package?
4. Courtney is making 72 cookies. She will make rectangles and cut them into triangles. Each rectangle will be 2 inches by 4 inches. What is the area of each cookie? If she wants to put icing on them, how many cans will she need if each can will cover 48 square inches?
5. Terry is selling plants from her garden. Buy 3/\$4.50 and get one free. Mrs. Greenthumb wants 20 plants; how much will she pay? How many plants would you get for \$27?
6. Heather and Holly were eating their lunch. First, 18 seagulls swooped down but 11 flew away. Then 12 more came and 2 flew away. Finally, 14 came to visit and 8 of those stayed. At this point, how many gulls were still on the beach?
7. Tim and his dad build a sandcastle. They start at 10:30AM and build for 2 hours and 15 minutes. What time are they finished? High tide comes in at 3:35 and washes their castle away. How long was the completed castle standing? Give the time in hours and minutes.
8. Umbrellas rent for \$3 a day. The Jacksons will be at the shore for 2 weeks. Should they buy an umbrella for \$34.95 or rent one everyday? Justify your answer.

10 most important mathematical concepts/skills that students should know and be able to do before entering Geometry

These concepts and skills serve as the foundation for what will be taught in Geometry.

Equations: Solve and graph two-step linear equations and inequalities, and equations and inequalities with variables on both sides.
Ratio: Understand the meaning and use of ratio, rates and proportions.
Graphing: Accurately plot ordered pairs, and graph linear equations and inequalities on a coordinate plane.
Slope: Explain the meaning of slope as a constant rate of change, and understand how to find the slope of a line.
Order of operations: Understand and use the order of operations to simplify expressions and perform calculations (with rational numbers, decimals, integers, integer exponents and radicals).
Square roots: Understand the meaning of a square root, and use them in calculations.
Translating information: Translate information from problem situations or statements into equations and inequalities.
Properties: Understand the distributive property and how to use it to simplify expressions, solve equations and multiply binomials.
Integers: Demonstrate fluency in computing with integers (add, subtract, multiply, divide) and simplifying algebraic expressions involving integers.
Measurement: Correctly use a ruler (standard and metric) to obtain measurements to a specific degree of accuracy, and use a protractor to measure angles.

Helpful websites:

<http://www.mathsisfun.com/>

www.webmath.com